



Limiting the Abundance of LIGO/Virgo Black Holes with Microlensing Observations of Quasars of Finite Size

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Abstract

We present a simple but general argument that strongly limits the abundance of primordial black holes (PBHs) (or other unknown population of compact objects) with masses similar to those determined by LIGO/Virgo from BH binary mergers. We show that quasar microlensing can be very sensitive to the mass of the lenses, and that it is able to distinguish between stars and BHs of high mass, when the finite size of the source is taken into account. A significant presence of massive BHs would produce frequent high-flux magnifications (except for unrealistically large sources), which have been very rarely observed. On the contrary, a typical stellar population would induce flux magnifications consistent with the observations. This result excludes PBHs (or any type of compact object) in the mass range determined by LIGO/Virgo as the main dark matter constituents in the lens galaxies.

Unified Astronomy Thesaurus concepts: [Cosmology \(343\)](#); [Dark matter \(353\)](#); [Primordial black holes \(1292\)](#); [Astrophysical black holes \(98\)](#); [Quasar microlensing \(1318\)](#); [Gravitational lensing \(670\)](#)

1. Introduction

The discovery of gravitational waves from binary black hole mergers by the LIGO/Virgo collaboration (see GWTC-1 and GWTC-2 by Abbott et al. 2019a and Abbott et al. 2021) with masses higher than previously expected for black holes (BHs) of stellar origin (but also the low effective spins of the components) renewed in the last years the interest in the possibility that some of these BHs were of primordial origin, and even that these primordial black holes of intermediate mass (20–200 M_{\odot}), not excluded by galactic microlensing, could constitute a significant fraction of the dark matter in the universe (Carr & Kühnel 2020; Blaineau et al. 2022).

Quasar microlensing (Chang & Refsdal 1979; Wambsgans 2006) provides an alternative path to study the abundance not only of BHs but also of any type of compact object. The description of this phenomenon is simple: An intervening galaxy (the lens) deflects the light from a distant quasar, forming several images. These images are usually seen through the lens galaxy and, as far as the matter distribution in the galaxy is not smooth but granulated in compact objects (stars, BHs, etc.), the light beams can suffer from new secondary deflections, producing several microimages (which cannot be resolved by telescopes). The primary observational effect of this image splitting is a change in the flux of the images (microlensing flux magnification). The relevant question we will address here is: Can the amplitude and frequency of these microlensing flux magnifications inform us about the mass of the microlenses? Or, more specifically: Can microlensing

observations unequivocally reveal the presence of LIGO/Virgo BHs?

Previous studies based on quasar microlensing (Mediavilla et al. 2017; Esteban-Gutiérrez et al. 2020) do not support the existence of a significant population of intermediate-mass BH. However, neither these negative results from microlensing nor the existence of new proposed paths to explain the stellar formation of BH of intermediate mass (see, e.g., Abbott et al. 2021) seems to have had a major impact in stopping speculation about the existence of a population of primordial black holes that could account for the dark matter. This fact may be related to the indirect approach and rather complex statistical modeling involved in those microlensing studies, which we intend to avoid here.

As we will discuss, the key parameter that determines the differences in amplitude and frequency of microlensing magnifications corresponding to populations of microlenses of different masses is the size of the lensed object, which in our case is the size of the quasar accretion disk at (rest-frame) UV wavelengths. The motivation of this work is, then, to show, using broadly applicable arguments, that quasar microlensing is very sensitive to the mass of BHs in the range of masses of LIGO/Virgo detections. Specifically, we will show that there is a strong difference in predicted microlensing magnifications for stars and LIGO/Virgo BHs when a source of finite size is considered. We leave a thorough statistical analysis with quantitative estimates of the limits in the abundance of BHs to an accompanying paper.

This Letter is organized as follows. In Section 2 we analyze the impact of the size of the source in the probability distribution of observing a given microlensing magnification and compare the results with available microlensing observations. In Section 3 we discuss the differences in microlensing of



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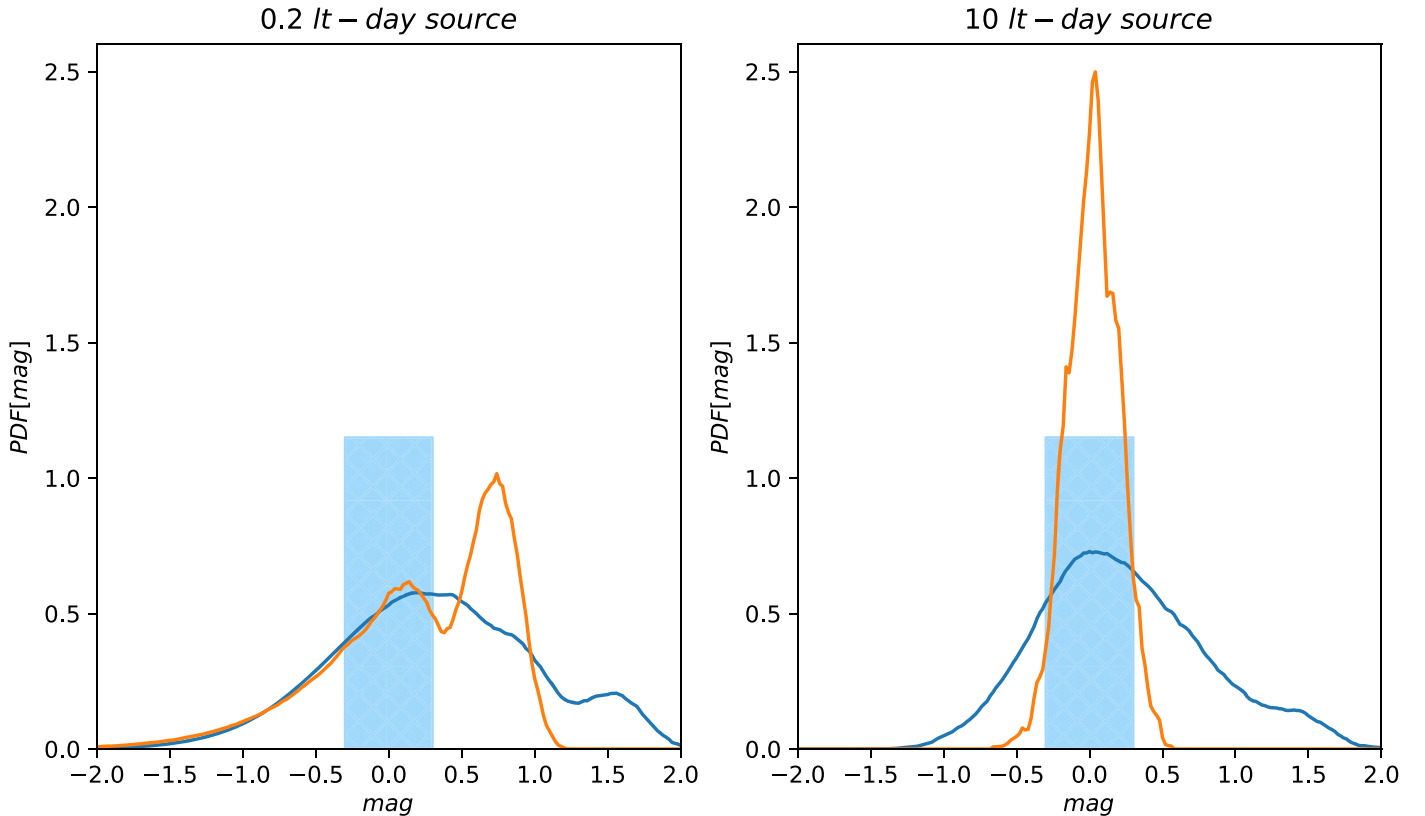


Figure 1. Probability distributions of microlensing flux magnifications for a population of 20% stars with $0.2M_{\odot}$ plus 80% smooth dark matter (orange curve) and a population of 20% stars with $0.2M_{\odot}$ plus 80% LIGO/Virgo-type BHs of $30M_{\odot}$ (blue curve). The left panel is for a source of 0.2 lt-days. The right panel is for a source of 10 lt-days. The scaling has been chosen to give the unit area under the PDF curves. The shaded blue area marks the region containing $\sim 70\%$ of the observed microlensing magnifications (Pooley et al. 2007), i.e., with the ordinate chosen to enclose 70% of the probability (see text).

quasars by stars or by LIGO/Virgo BHs. Finally, in this same section (Section 3), we summarize the conclusions.

2. Results

We want to study the impact of the mass of microlenses on both the amplitude and frequency of magnifications, focusing on to what extent a population of LIGO/Virgo-type BHs can account for the unrevealed dark matter in the lens galaxies. To do that, we are going to calculate the probability of measuring a given microlensing flux magnification for two different populations of microlenses, both with 20% of their matter in stars (with $m = 0.2M_{\odot}$, typical of old stellar populations), but one with the remaining 80% of matter in smooth dark matter⁸ and the other in typical LIGO/Virgo BHs with $m = 30M_{\odot}$. Following the standard procedure, we obtain the probability density function (PDF) of the flux magnification from the histogram of the magnification maps.⁹ In these calculations, we have considered a typical lens system¹⁰ with a mean flux magnification of 10. We use a pixel size of 0.2 lt-days for the magnification maps, very much smaller than typical quasar sizes. The PDFs from measuring a certain flux magnification for both mass distributions are shown in Figure 1 (left). Both PDFs match very well

in the negative magnitude region (corresponding to microlensing flux increase), although they show clear differences in the positive wing (corresponding to a flux decrease).

It is worth wondering, at this point, how well these probability distributions compare to actual observations. The optical fluxes (normalized to their expected model values) reported by Pooley et al. (2007; their Table 5) for nine¹¹ quadruple lens systems are very well suited for a quick comparison. While according to Pooley et al. (2007) $\sim 70\%$ of the observed magnifications fall in the $(-0.3, 0.3)$ mag range (region shaded in blue in Figure 1) our simulations for an infinitesimal source predict only $\sim 30\%$ of measurements in this range. As we will see below, this strong discrepancy originates from the fact that real quasars have sizes much larger than the pixel size used in our calculations. To take this fact into account, we can calculate the corresponding probability distributions for an extended source. We have chosen here to model the source with a Gaussian brightness profile, but this is known to have little effect on the microlensing magnification probability distributions (Mortonson et al. 2005; Muñoz et al. 2016). We consider a source size of 10 lt-days, which approximates the Einstein radius (the natural length scale of lensing) of the $m = 0.2M_{\odot}$ stars, yet it is much smaller than the Einstein radius of the BHs (~ 112 lt-days). Nevertheless, the conclusions remain essentially unchanged for any reasonable source size compatible with observations.

⁸ This is the typical baseline scenario (Schechter et al. 2014; Jiménez-Vicente et al. 2015a, 2015b) in which the population of microlenses contributes 20% to the total mass density (including dark matter) and the remaining 80% is in the form of a smooth distribution of matter.

⁹ Obtained by tracing light rays backward from the image to the source through the random distribution of microlenses (Kayser et al. 1986).

¹⁰ We take $\kappa = \gamma = 0.45$, $z_l = 0.5$, and $z_s = 2$.

¹¹ We have eliminated Q2237+0305 from their sample in this comparison, as this system is produced by a nearby lens and has nearly 100% of its mass density in the form of compact objects.

The resulting probability distributions for this larger source are shown in Figure 1 (right). In this figure, it can be clearly seen that while the PDF of the stars becomes significantly narrower (therefore predicting less extreme magnifications, in better agreement with observations), the PDF of the BHs has changed much less (still predicting over $\sim 60\%$ of magnifications outside the $(-0.3, 0.3)$ mag range). The reason for this different behavior is indeed rather simple: For a finite source size, the gradients in the magnification maps produced by lenses with an Einstein radius comparable to the source size get blurred/averaged, while this effect is minimized if the source has a negligible size compared to the Einstein radius of the lens.

We would like to stress again that although we have chosen here some values of the parameters to illustrate the principle, this result is, nevertheless, very general and has little dependence on the specific choice as long as it is in reasonable agreement with observations.

3. Discussion and Conclusions

An immediate result of the previous section is that we need to consider sizes of quasars comparable to the Einstein radius of the lenses in order to narrow the predicted PDF to approximate (even roughly) the experimental histogram of microlensing magnifications. If BHs were to account for a significant fraction of the mass in lens galaxies, this would imply source sizes of $\gtrsim 100$ lt-days, which is absolutely discarded by reverberation-mapping estimates of the size of the accretion disks of quasars (see, e.g., Edelson et al. 2015; Fausnaugh et al. 2016; Jiang et al. 2017; Cackett et al. 2018; Homayouni et al. 2019 and Yu et al. 2020). On the contrary, for typical estimated sizes of quasar accretion disks at these wavelengths of a few light-days, the PDF predicted by a population of stars is reasonably consistent with the observations. Therefore, if the dark matter of the lens galaxies were in the form of BHs of the masses detected by LIGO/Virgo, much larger microlensing magnifications should have been regularly observed. As this is not the case, a dark-matter-based explanation for these kinds of objects can safely be discarded.

On the other hand, although we have used here for comparison the estimates of microlensing magnifications from Pooley et al. (2007) (because the reported observed fluxes normalized to model predictions directly provide the flux magnifications), the rarity of high-flux magnifications is also extensively confirmed by the statistics of differential flux magnifications between images (Mediavilla et al. 2009; Fian et al. 2016, 2018) and by the microlensing-induced variability observed in the light curves of lensed quasar images (see, e.g., Mediavilla et al. 2016 and references therein).

Regarding the possibility of a partial explanation of dark matter in terms of LIGO/Virgo BHs, we have also calculated the PDFs of populations including less than 80% of BHs, down to just 10%, and confirmed the significant overprediction of unobserved large microlensing magnifications, even for this small abundance of BHs. In an accompanying paper, we discuss the likelihood of a population of BHs in all ranges of BH abundances.

From the above analysis, we can reach the following conclusions:

1. The observed microlensing magnification statistics in optical observations of lensed quasars can only be explained if the source (the quasar accretion disk) size is comparable to the Einstein radius of the microlenses.

2. For reasonable values of the size of the observed quasars, if the dark matter were in the form of compact objects with masses in the range of the BHs detected by LIGO/Virgo, much larger magnifications should have been frequently observed. The absence of such observations is therefore strong proof that the dark matter in lens galaxies is not formed by these objects.

The above conclusions are based on very general arguments that do not depend on specific models. Nevertheless, a full quantitative Bayesian statistical modeling of a mixed population of stars and BHs setting quantitative limits on the abundance of the latter is included in an accompanying paper.

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References

- Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2019a, *PhRvX*, 9, 031040
- Abbott, R., Abbott, T. D., Abraham, S., et al. 2021, *PhRvX*, 11, 021053
- Abbott, R., Abbott, T. D., Abraham, S., et al. 2021, *ApJL*, 913, L7
- Blaineau, T., Moniez, M., Afonso, C., et al. 2022, arXiv:2202.13819
- Cackett, E. M., Chiang, C.-Y., McHardy, I., et al. 2018, *ApJ*, 857, 53
- Carr, B., & Kühnel, F. 2020, *ARNPS*, 70, 355
- Chang, K., & Refsdal, S. 1979, *Natur*, 282, 561
- Edelson, R., Gelbord, J. M., Horne, K., et al. 2015, *ApJ*, 806, 129
- Esteban-Gutiérrez, A., Agües-Paszukowsky, N., Mediavilla, E., et al. 2020, *ApJ*, 904, 176
- Fausnaugh, M. M., Denney, K. D., Barth, A. J., et al. 2016, *ApJ*, 821, 56
- Fian, C., Mediavilla, E., Hanslmeier, A., et al. 2016, *ApJ*, 830, 149
- Fian, C., Mediavilla, E., Jiménez-Vicente, J., et al. 2018, *ApJ*, 869, 132
- Homayouni, Y., Trump, J. R., Grier, C. J., et al. 2019, *ApJ*, 880, 126
- Jiang, Y.-F., Green, P. J., Greene, J. E., et al. 2017, *ApJ*, 836, 186
- Jiménez-Vicente, J., Mediavilla, E., Kochanek, C. S., & Muñoz, J. A. 2015a, *ApJ*, 799, 149
- Jiménez-Vicente, J., Mediavilla, E., Kochanek, C. S., & Muñoz, J. A. 2015b, *ApJ*, 806, 251
- Kayser, R., Refsdal, S., & Stabell, R. 1986, *A&A*, 166, 36–52
- Mediavilla, E., Jiménez-Vicente, J., Muñoz, J. A., et al. 2016, *ApJ*, 832, 46
- Mediavilla, E., Jiménez-Vicente, J., Muñoz, J. A., et al. 2017, *ApJL*, 836, L18
- Mediavilla, E., Muñoz, J. A., Falco, E., et al. 2009, *ApJ*, 706, 1451
- Mortonson, M. J., Schechter, P. L., & Wambsganss, J. 2005, *ApJ*, 628, 594
- Muñoz, J. A., Vives-Arias, H., Mosquera, A. M., et al. 2016, *ApJ*, 817, 155
- Pooley, D., Blackburne, J. A., Rappaport, S., et al. 2007, *ApJ*, 661, 19
- Schechter, P. L., Pooley, D., Blackburne, J. A., & Wambsganss, J. 2014, *ApJ*, 793, 96
- Wambsganss, J. 2006, Saas-Fee Advanced Course: Gravitational Lensing: Strong, Weak and Micro, 33 ed. G. Meylan, P. Jetzer, & P. North (Berlin: Springer), 453
- Yu, Z., Martini, P., Davis, T. M., et al. 2020, *ApJS*, 246, 16